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AUTHORS:

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TITLE:

Reflection and transmission of a plane-parallel layer in the scope of non-linear optics

PERIODICAL: Inzhenerno-fizicheskiy zhurnal, v. 5, no. 10, 1962, 58 - 64

TEXT: The subject of investigation is a plate of thickness 1 and of small luminance characterized by the absorption coefficient k_0 and the reflection coefficient on the face r. A luminous flux S_0 is incident perpendicularly. Owing to multiple reflection there exist internally two kinds of flux at any point $x:S_1$ moving parallel to the incident flux and S_2 moving in the opposite direction. These are described by the differential equations $dS_1 = -kS_1dx$, $dS_2 = kS_2dx$ (1) with the boundary conditions $S_1(x=0) = S_0(1-r) + rS_2(x=0)$, $S_2(x=1) = rS_1(x=1)$ (2). The absorption coefficient can be expressed by $k = k_0/1 + \alpha(S_1 + S_2)$, where Card 1/4

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the parameters of non-linearity α and k_0 are assumed to be constant with respect to depth. The system (1) is solved by

$$\ln C_2 \alpha S_1 + \alpha S_1 - \frac{C_1}{\alpha S_1} = -k_0 x, \quad \ln \frac{\alpha S_2}{C_1 C_2} + \alpha S_2 - \frac{C_1}{\alpha S_2} = k_0 x. \tag{4}$$

and the relation $S_1S_2 = C_1/\alpha^2$ can be derived additionally from (1), stating that the product of two oppositely directed fluxes is constant at any depth. Hence the reflection coefficient R is obtained by

$$R = \frac{(1-r)C_1}{\alpha S_0 A} + r. \tag{8}$$

and the transmission factor T by

$$T = \frac{1 - r}{\alpha S_0} \sqrt{\frac{C_1}{r}} \tag{9}.$$

On the basis of these formulas the light field was studied inside and outside the medium. For the region where k is positive R and T are calculated by

$$R = r + \frac{(1-r)^2 r \exp(-2k_b l)}{1-r^2 \exp(-2k_b l)}, \quad T = \frac{(1-r)^2 \exp(-k_b l)}{1-r^2 \exp(-2k_b l)}$$
(10)

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for the condition $\alpha S_0 \ll 1$, and by

$$R = \frac{2r}{1+r} - \frac{2r}{\alpha S_0 (1+r)^3} k_0 l,$$

$$T = \frac{1-r}{1+r} - \frac{1}{\alpha S_0} k_0 l$$
(11)

for the condition $\alpha S_0 \gg 1$. For the region of negative values of k_0 ,

$$R = \frac{2\alpha S_0 k_0 (r - 2r(1-r) (\alpha S_0)^2 - r(k_0 l)^2}{\alpha S_0 [2k_0 lr - \alpha S_0 (1-r^2)]},$$

$$T = \frac{(1-r^2) k_0 l \alpha S_0 - (1-r)^2 (\alpha S_0)^2 - r(k_0 l)^2}{\alpha S_0 [2k_0 lr - \alpha S_0 (1-r^2)]}$$
(14)

holds for high luminances. At high values of r the energy density distribution in the plate is virtually constant. At small values, this distribution has a minimum in the interior of the plate which vanishes if $r \rightarrow 1$. There are 4 figures.

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